

page 110 WARM UP: Copy below and then do #2.

Example 2: What if the terms aren't lined up?

Use algebra to rearrange the terms until they are all lined up!

$$1. \begin{cases} 2y = -x + 7 \\ 3x - 2y = -3 \end{cases}$$

$$\begin{array}{r} 2y = -x + 7 \\ +x \quad +x \\ \hline x + 2y = 7 \end{array}$$

$$\begin{array}{r} x + 2y = 7 \\ 3x - 2y = -3 \\ \hline 4x = 4 \end{array}$$

$$\begin{array}{r} 4x = 4 \\ x = 1 \end{array}$$

$(1, 3)$

$$\begin{array}{r} 2y = -x + 7 \\ 2y = -(1) + 7 \\ 2y = -1 + 7 \\ 2y = 6 \\ y = 3 \end{array}$$

$$2. \begin{cases} 3x + 7y = 48 \\ 5x = 7y - 32 \end{cases}$$

$$\begin{array}{r} 3x + 7y = 48 \\ 5x - 7y = -32 \\ \hline 8x = 16 \\ x = 2 \end{array}$$

$$\begin{array}{r} 3(2) + 7y = 48 \\ 6 + 7y = 48 \\ 7y = 42 \\ y = 6 \end{array}$$

$(2, 6)$

1.  $\begin{cases} 2y = -x + 7 \\ 3x - 2y = -3 \end{cases}$

$$\begin{array}{r} 2y = -x + 7 \\ +x \quad +x \\ \hline x + 2y = 7 \\ 3x - 2y = -3 \\ \hline 4x = 4 \\ x = 1 \end{array}$$

$2y = -x + 7$   
 $2y = -(1) + 7$   
 $2y = -1 + 7$   
 $2y = 6$   
 $y = 3$


$(1, 3)$

2.  $\begin{cases} 3x + 7y = 48 \\ 5x = 7y - 32 \end{cases}$

$$\begin{array}{r} 3x + 7y = 48 \\ -7y \quad -7y \\ \hline 5x - 7y = -32 \\ 3x + 7y = 48 \\ \hline 8x = 16 \\ x = 2 \end{array}$$

$3x + 7y = 48$   
 $3(2) + 7y = 48$   
 $6 + 7y = 48$   
 $7y = 42$   
 $y = 6$

$(2, 6)$

 [http://www.youtube.com/watch?feature=player\\_detailpage&v=1qHTmxlaZWQ](http://www.youtube.com/watch?feature=player_detailpage&v=1qHTmxlaZWQ)

## answers HW page 62 &amp; 63

<p>1. <math>\begin{cases} 7x + 2y = 10 \\ -x + y = -16 \end{cases} +</math></p> $\begin{array}{r} 7x + 2y = 10 \\ -x + y = -16 \\ \hline 3y = -6 \\ y = -2 \end{array}$ <p><math>7x + 2(-2) = 10</math>  <math>7x - 4 = 10</math>  <math>7x = 14</math>  <math>x = 2</math></p> <p><math>(2, -2)</math></p>	<p>2. <math>\begin{cases} 8x + 11y = 20 \\ 5x - 11y = -59 \end{cases} +</math></p> $\begin{array}{r} 8x + 11y = 20 \\ 5x - 11y = -59 \\ \hline 13x = -39 \\ x = -3 \end{array}$ <p><math>8(-3) + 11y = 20</math>  <math>-24 + 11y = 20</math>  <math>11y = 44</math>  <math>y = 4</math></p> <p><math>(-3, 4)</math></p>	<p>3. <math>\begin{cases} -4x - 3y = -15 \\ 4x - 7y = -15 \end{cases}</math></p> $\begin{array}{r} -4x - 3y = -15 \\ 4x - 7y = -15 \\ \hline -10y = -30 \\ y = 3 \end{array}$ <p><math>-4x - 3(3) = -15</math>  <math>-4x - 9 = -15</math>  <math>-4x = -6</math>  <math>x = \frac{3}{2}</math></p> <p><math>(\frac{3}{2}, 3)</math> or <math>(1\frac{1}{2}, 3)</math></p>
<p>4. <math>\begin{cases} 2x + 6y = 20 \\ -x - 5y = 12 \end{cases} +</math></p> $\begin{array}{r} 2x + 6y = 20 \\ -x - 5y = 12 \\ \hline y = 32 \end{array}$ <p><math>2x + 6(32) = 20</math>  <math>2x + 192 = 20</math>  <math>-192 - 192</math>  <math>\frac{2x}{2} = \frac{-172}{2}</math>  <math>x = -86</math></p> <p><math>(-86, 32)</math></p>	<p>5. <math>\begin{cases} 3x + 6y = 6 \\ 4x - 6y = 8 \end{cases}</math></p> $\begin{array}{r} 3x + 6y = 6 \\ 4x - 6y = 8 \\ \hline 7x = 14 \\ x = 2 \end{array}$ <p><math>3(2) + 6y = 6</math>  <math>6 + 6y = 6</math>  <math>6y = 0</math>  <math>y = 0</math></p> <p><math>(2, 0)</math></p>	<p>6. <math>\begin{cases} 6x - 8y = 40 \\ 5x + 8y = 48 \end{cases}</math></p> $\begin{array}{r} 6x - 8y = 40 \\ 5x + 8y = 48 \\ \hline 11x = 88 \\ x = 8 \end{array}$ <p><math>6(8) - 8y = 40</math>  <math>48 - 8y = 40</math>  <math>-8y = -8</math>  <math>y = 1</math></p> <p><math>(8, 1)</math></p>

<p>1. <math>\begin{cases} 7x - 3y = -39 \\ 3(x + y = -9) \end{cases}</math></p> $\begin{array}{r} 7x - 3y = -39 \\ 15x + 3y = -27 \\ \hline 22x = -66 \\ x = -3 \end{array}$ <p><math>7(-3) - 3y = -39</math>  <math>-21 - 3y = -39</math>  <math>-3y = -18</math>  <math>y = 6</math></p> <p><math>(-3, 6)</math></p>	<p>2. <math>\begin{cases} 3x + 2y = 17 \\ 2(x - y = 2) \end{cases}</math></p> $\begin{array}{r} 3x + 2y = 17 \\ 4x - 2y = 4 \\ \hline 7x = 21 \\ x = 3 \end{array}$ <p><math>3(3) + 2y = 17</math>  <math>9 + 2y = 17</math>  <math>2y = 8</math>  <math>y = 4</math></p> <p><math>(3, 4)</math></p>	<p>3. <math>\begin{cases} 2x + 5y = 10 \\ -2(x + 3y = 7) \end{cases}</math></p> $\begin{array}{r} 2x + 5y = 10 \\ -2x - 6y = -14 \\ \hline -y = -4 \\ y = 4 \end{array}$ <p><math>2x + 5(4) = 10</math>  <math>2x + 20 = 10</math>  <math>2x = -10</math>  <math>x = -5</math></p> <p><math>(-5, 4)</math></p>
<p>4. <math>\begin{cases} 5(x + 2y = -2) \\ 5x + 3y = -17 \end{cases}</math></p> $\begin{array}{r} -5x - 10y = 10 \\ 5x + 3y = -17 \\ \hline -7y = -7 \\ y = 1 \end{array}$ <p><math>5x + 3(1) = -17</math>  <math>5x + 3 = -17</math>  <math>5x = -20</math>  <math>x = -4</math></p> <p><math>(-4, 1)</math></p>	<p>5. <math>\begin{cases} x + 4y = 6 \\ 4(2x - y = -6) \end{cases}</math></p> $\begin{array}{r} x + 4y = 6 \\ 8x - 4y = -24 \\ \hline 9x = -18 \\ x = -2 \end{array}$ <p><math>-2 + 4y = 6</math>  <math>4y = 8</math>  <math>y = 2</math></p> <p><math>(-2, 2)</math></p>	<p>6. <math>\begin{cases} -2x - y = 3 \\ 3x + 5y = 6 \end{cases}</math></p> $\begin{array}{r} -10x - 5y = 15 \\ 3x + 5y = 6 \\ \hline -7x = 21 \\ x = -3 \end{array}$ <p><math>3(-3) + 5y = 6</math>  <math>-9 + 5y = 6</math>  <math>5y = 15</math>  <math>y = 3</math></p> <p><math>(-3, 3)</math></p>

Multiply **both** lines through by a factor that will force a variable to cancel when the lines are added:

$$\begin{array}{l} 7. \quad 3(5x + 4y = 22) \\ \quad 4(3x - 3y = -3) \end{array}$$

$$\begin{array}{r} 15x + 12y = 66 \\ 12x - 12y = -12 \\ \hline 27x = 54 \end{array}$$

$$(x = 2)$$

$$5(2) + 4y = 22$$

$$10 + 4y = 22$$

$$\xrightarrow{-10} -10$$

$$\frac{4y = 12}{4 \quad 4}$$

$$(y = 3)$$

$$(2, 3)$$

$$\begin{array}{l} 8. \quad 3(5x - 2y = -12) \\ \quad 2(2x + 3y = -1) \end{array}$$

$$\begin{array}{r} 15x - 6y = -36 \\ 4x + 6y = -2 \\ \hline 19x = -38 \end{array}$$

$$(x = -2)$$

$$5(-2) - 2y = -12$$

$$-10 - 2y = -12$$

$$\xrightarrow{+10} +10$$

$$-2y = -2$$

$$(y = 1)$$

$$(-2, 1)$$

$$\begin{array}{l} 9. \quad 5(4x - 2y = 20) \\ \quad -2(-3x - 5y = -2) \end{array}$$

$$\begin{array}{r} 20x - 10y = 100 \\ 6x + 10y = 4 \\ \hline 26x = 104 \end{array}$$

$$(x = 4)$$

$$4(4) - 2y = 20$$

$$16 - 2y = 20$$

$$\xrightarrow{-16} -16$$

$$-2y = 4$$

$$(y = -2)$$

$$(4, -2)$$

**Example 3: What if the terms are lined up, and could cancel except that the signs aren't right?**

Then you can \_\_\_\_\_ the lines instead.

Basically multiply the left and right side of one of the lines by \_\_\_\_\_.

$$1. \begin{cases} 2x + 7y = 12 \\ 2x + 3y = 4 \end{cases} \quad \begin{cases} 6x - 8y = 40 \\ -5x - 8y = -48 \end{cases}$$

**✓ Understanding Check:**

$$a. \begin{cases} 10x - 4y = 6 \\ 10x + 3y = 13 \end{cases}$$

$$b. \begin{cases} -2x + 3y = -9 \\ x + 3y = 3 \end{cases}$$

page 113

Writing Equations in  $Ax + By = C$  to describe real situations:Write an equation in  $Ax + By = C$  for each situation:

1. A company will charge \$3 to ship a medium size box to China, and \$4 to ship a large box to China. Write an equation to represent the amount of boxes the company could ship if their shipping budget is 132 dollars.

Define your variables:

Let  $x =$  # med boxesLet  $y =$  # lg boxes

Equation:  $3x + 4y = 132$

2. Jenny is making a scrapbook of her senior year. She needs to get some pictures printed. She finds an online company that will print and send her 3x5 pictures for 20¢ each and 4x6 pictures for 30¢ each. If she is only allowed to order \$10.00 worth of pictures, write an equation to represent the amount of each size of picture she could order.

Define your variables:

Let  $s =$  # of 3x5 picsLet  $L =$  # of 4x6 pics

Equation:  $20s + 30L = 10$

$20s + 30L = 1000$



3. Jeff is packing a care box to send to his brother who is a soldier. He wants to send him his favorite cookies which weigh 10 oz. each and winter socks which weigh 22 oz per pair. He has been told that his box can weigh 8 pounds. Write an equation to represent the number of boxes of cookies and pairs of socks Jeff could pack for his brother. (Careful! The units must match, 1 lb = 16 oz)

Define your variables:

Let  $C$  = # cookies  
Let  $S$  = # pairs of socks

Equation:  $10C + 22S = 128$

4. Julie is trying to lose weight. She decides to try to burn calories by walking or jogging. She finds out that walking burns an average of 5 calories per minute, and jogging burns an average of 7 calories per minute. Write an equation to show the amount of walking or jogging Julie would need to do to burn an extra 300 calories.

Define your variables:

Let  $W$  = time walked (min)  
Let  $J$  = min jog

Equation:  $5W + 7J = 300$

page 114

### 6-4 More Applications of Linear Systems

#### Example 1: Standard Form System

A necklace with 6 large beads and 30 small beads weighs 78 grams. A bracelet with 3 large beads and 10 small beads weighs 29 grams. Write and solve a system to find out how much large beads weigh and how much small beads weigh.

Define the variables: Let  $L$  = weight of Lg beads  
Let  $S$  = weight of Sm bead

Write an equation for the necklace:  $6L + 30S = 78$

Write an equation for the bracelet:  $3L + 10S = 29$

Use the elimination method to solve the problem:

$$\begin{array}{r}
 6L + 30S = 78 \\
 -6L - 20S = -58 \\
 \hline
 10S = 20 \\
 \textcircled{S=2}
 \end{array}$$

$$\begin{array}{r}
 6L + 30(2) = 78 \\
 6L = 18 \\
 \textcircled{L=3}
 \end{array}$$

The sm beads weigh 2 oz and  
the Lg beads weigh 3 oz.

**Example 2: Ticket Problem**

Suppose your community center sells a total of 292 tickets for a basketball game. An adult ticket costs \$3. A student ticket costs \$1. The sponsors collect \$470 in ticket sales. Write and solve a system to find the number of each type of tickets sold?

Define the variables: Let  $A$  = # of adult tix sold  
 Let  $S$  = # of student tix sold

Write an equation for the total number of tickets:  $A + S = 292$

Write an equation for the total amount of sales:  $3A + S = 470$

Use the elimination method to solve the problem:

$$89 + S = 292$$

$$S = 203$$

89 adult tix and 203 student tix were sold.

$$-A - S = -292$$

$$3A + S = 470$$

$$2A = 178$$

$$A = 89$$

**Example 3: Sales Problem**

page 115

Suppose your class sells gift wrap for \$4 per package and greeting cards for \$10 per package. Your class sells 205 packages in all and receives a total of \$1084. Find the number of packages sold.

Define the variables: Let  $W$  = # gift wrap packages sold

Let  $C$  = # greeting card packages sold

Write an equation for the total number of packages:  $W + C = 205$

Write an equation for the total amount of sales:  $4W + 10C = 1084$

Use the elimination method to solve the problem:

We sold 161 packs of gift wrap and 44 packs of cards.

$$-10W - 10C = -2050$$

$$4W + 10C = 1084$$

$$-6W = -966$$

$$W = 161$$

$$161 + C = 205$$

$$C = 44$$

✓ Understanding Check:

Suppose another class sells a different brand of gift wrap, which costs \$2 per package, and cards, which cost \$5 per package. The class sells 250 packages in all and earns a total of \$695. Find the number of each type of package sold.

Define the variables: Let  $W$  = packs wrap  
Let  $C$  = packs cards

total number of packages:  $W + C = 250$   
total amount of sales:  $2W + 5C = 695$

Use the elimination method to solve the problem:

✓ Understanding Check:

Suppose another class sells a different brand of gift wrap, which costs \$2 per package, and cards, which cost \$5 per package. The class sells 250 packages in all and earns a total of \$695. Find the number of each type of package sold.

Define the variables: Let  $w$  = gift wrap  
 Let  $c$  = greeting cards

total number of packages:  $w + c = 250$   
 total amount of sales:  $2w + 5c = 695$

Use the elimination method to solve the problem:

$$\begin{array}{r} -2 \left( \begin{array}{l} w + c = 250 \\ 2w + 5c = 695 \end{array} \right) \end{array}$$

$$\begin{array}{r} -2w - 2c = -500 \\ 2w + 5c = 695 \end{array}$$

$$\frac{3c = 195}{3}$$

$$c = 65$$

$$\begin{array}{r} w + 65 = 250 \\ \quad \quad \quad \rightarrow 65 \\ \hline w = 185 \end{array}$$

They sold 65 packages of cards and 185 packages of gift wrap.

115

page 116

**Example 4: Coin/Value Problems**

You have 28 coins that are all nickels (n) and dimes (d). The value of the coins is \$2.05. How many of each coin do you have?

Define the variables: Let  $\underline{n}$  = # nickels  
Let  $\underline{d}$  = # dimes

Write an equation for the number of coins:  $n + d = 28$   
Write an equation for the value of the coins:  $5n + 10d = 205$

Solve the system using the equations:

**✓ Understanding Check:**

You have 15 coins in your pocket that are either quarters or nickels. They total \$2.75. How many of each coin do you have?

Define the variables:    Let \_\_\_\_\_ = \_\_\_\_\_  
                                    Let \_\_\_\_\_ = \_\_\_\_\_

Write an equation for the number of coins: \_\_\_\_\_

Write an equation for the value of the coins: \_\_\_\_\_

Solve the system using the equations:



You have 15 coins in your pocket that are either quarters or nickels. They total \$2.75. How many of each coin do you have?

Define the variables: Let  $n$  = nickels  
Let  $q$  = quarters

Write an equation for the number of coins:  $n + q = 15$

Write an equation for the value of the coins:  $.05n + .25q = 2.75$

Solve the system using the equations:

$$\begin{array}{r} -5(n + q = 15) \\ 100(.05n + .25q = 2.75) \end{array}$$

$$\begin{array}{r} -5n - 5q = -75 \\ 5n + 25q = 275 \\ \hline 20q = 200 \\ q = 10 \end{array}$$

$$n + 10 = 15$$

$$n = 5$$

There are 5 nickels and 10 quarters.

116

